



Wireless & Mobile Communications Lab

COST IC1102

4th Meeting

Thessaloniki, 22-24 May 2013

Performance of MISO Beamforming Systems based on Effective Radiation Patterns

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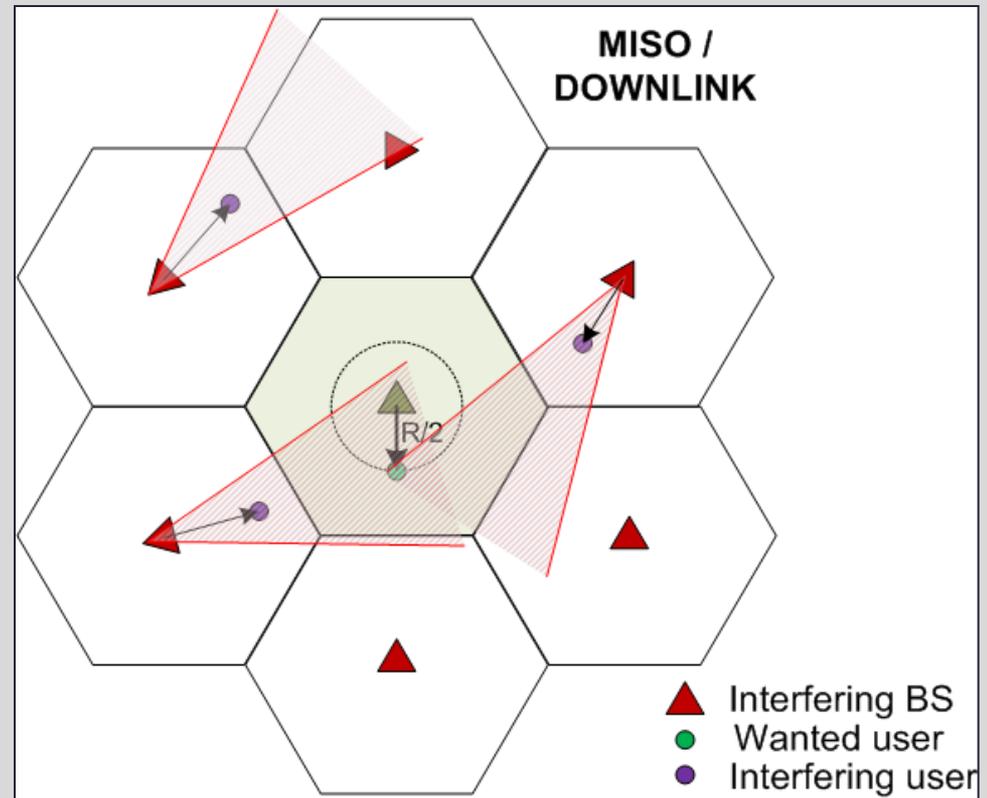


Presentation Outline

- System Description
- Problem formulation and solution
- SIR Gain estimations in multicarrier MISO beamforming systems
- Effective Radiation Pattern
- Choosing the appropriate Effective BW and Effective SLL

System Description

- Downlink
- Multicarrier
- 100% Loading Factor
- MISO beamforming
- All BS employ the same antenna radiation pattern
- Uniform distributed users



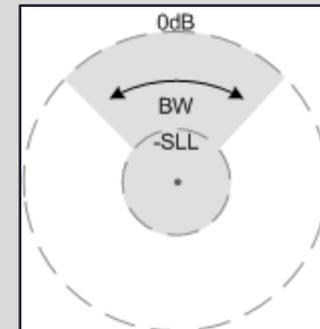
The Problem

➤ What is the SIR distribution in such a system?

$$SIR = \frac{P_0 G_{u,b_0} d_{u,b_0}^{-n} L_{u,0}}{\sum_{i \in I} P_0 G_{u,b_i} d_{u,b_i}^{-n} L_{u,b_i}}$$

➤ When,

- u : wanted user located at $R/2$ in the central cell
- L_{u,b_i} : shadowing effect, follows $\text{LogNormal}(0, \sigma)$
- The BSs employ the same *effective radiation pattern*.



The Solution (1)

$$\Pr(SIR < x_{SIR}, SLL) = \sum_{k=0}^6 P_k \Pr(SIR < x_{SIR}, SLL / k)$$

$$P_k = \binom{6}{k} p^k (1-p)^{6-k}$$

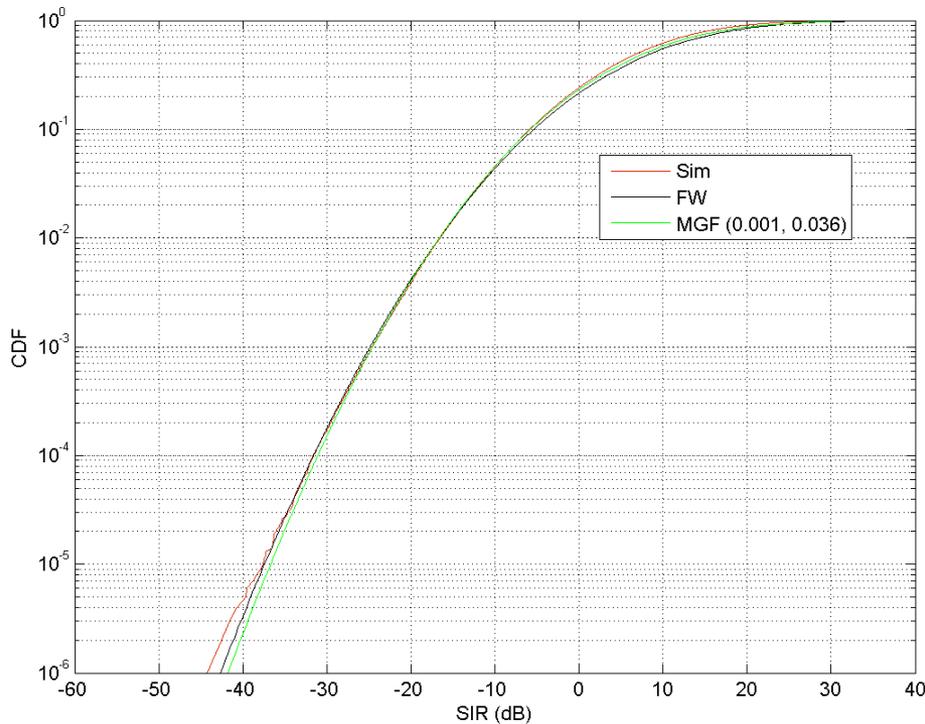
$$\Pr(SIR < x_{SIR}, SLL / k) = \Pr \left[\left(\frac{P_0 d_0^{-n} L_0}{\sum_{i=1}^k P_0 d_i^{-n} L_i + \sum_{j=1}^{6-k} P_0 d_j^{-n} L_j 10^{-\frac{SLL}{10}}} \right) < x_{SIR} \right]$$

➤ Sum of 6 LogN distributions

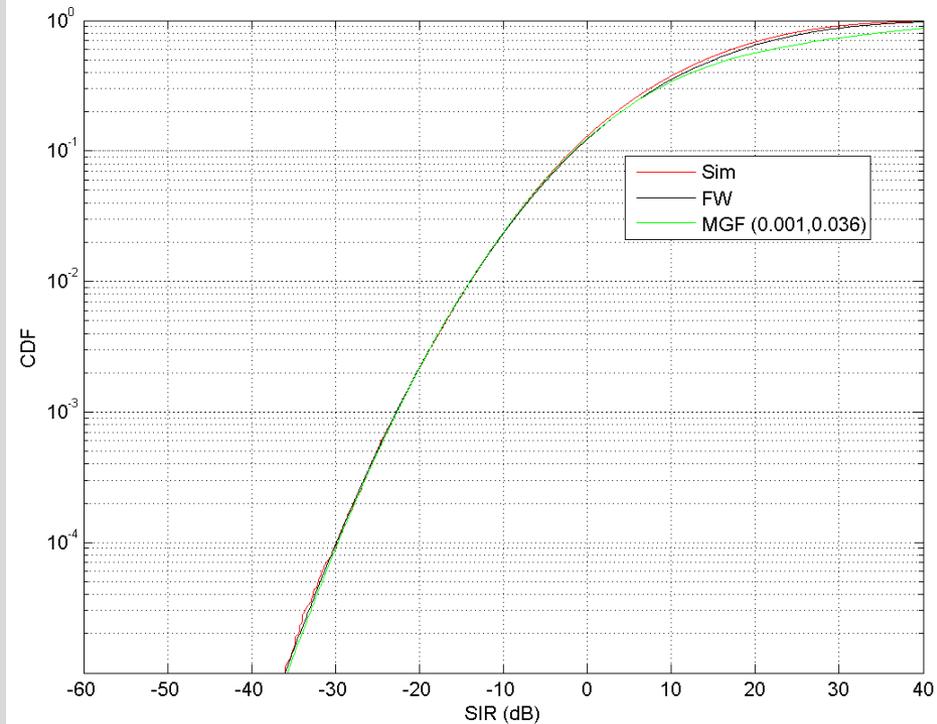
- Fenton-Wilkinson
- MGF (0.001-0.036)

The Solution (2)

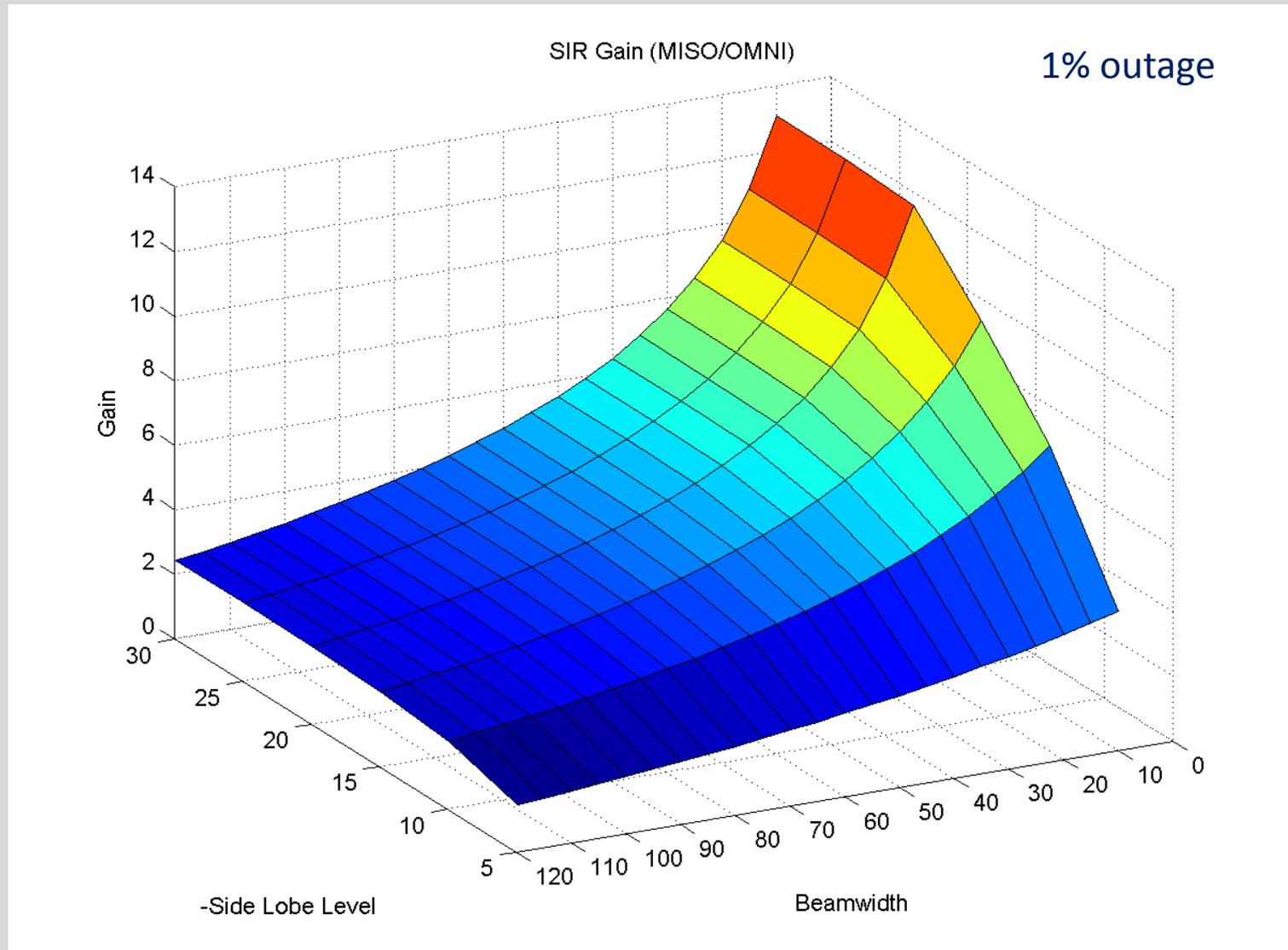
BW = 120°, SLL = -10dB



BW=60°, SLL=-20dB



SIR gain in MISO Beamforming Systems



Effective Radiation Pattern (1)

- The **Effective Radiation Pattern (ERP)** models the result of the convolution of the power azimuth spectrum with the ideal antenna pattern.
- The environment is modeled with the Laplace Distribution.
- So, the actual radiation pattern of an N -element array is:

$$G_{real}(\varphi_0) = \frac{1}{\sqrt{2}\sigma} \int_0^\pi \left| \frac{\sin\left(\frac{N}{2} \cos \varphi\right)}{\frac{N}{2} \pi \cos \varphi} \right| e^{-\frac{\sqrt{2}|\varphi - \varphi_0|}{\sigma}} d\varphi$$

Effective Radiation Pattern (2)

- Our goal is to model G_{real} with an ERP, G_{eff} .

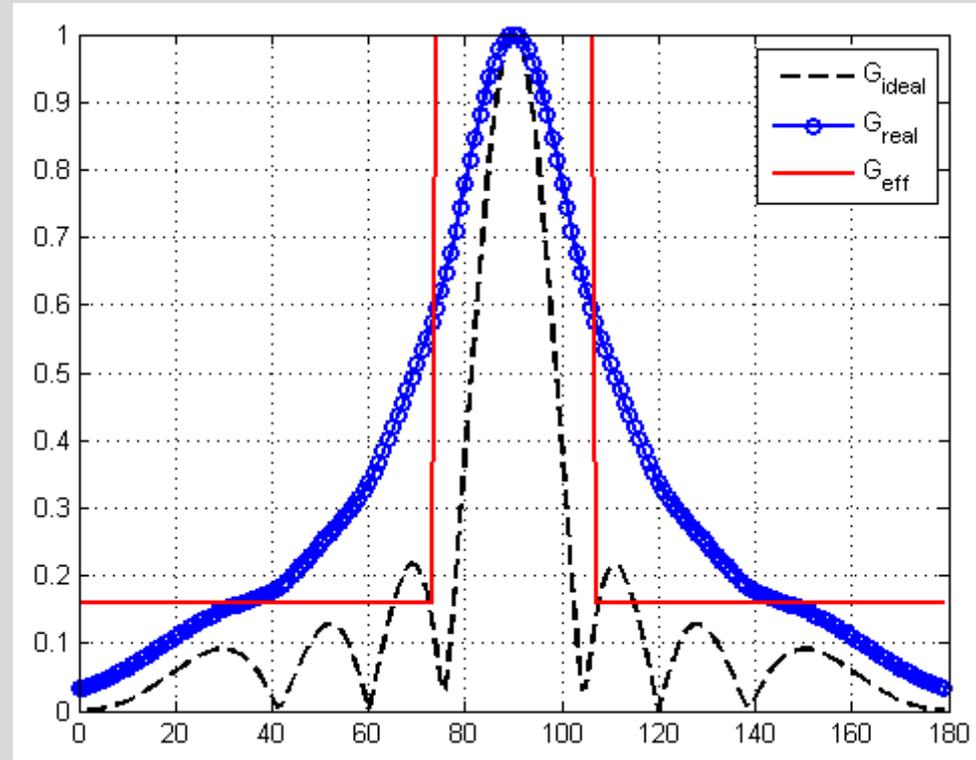
$$G_{\text{eff}} = \begin{cases} 1 & \varphi \in \left[\varphi_m - \frac{BW}{2}, \varphi_m + \frac{BW}{2} \right] \\ 10^{-\frac{SLL}{10}} & \varphi \in \left(0, \varphi_m - \frac{BW}{2} \right) \cup \left(\varphi_m + \frac{BW}{2}, \pi \right) \end{cases}$$

- So as to minimize the optimization function:

$$\{BW_{\text{opt}}, SLL_{\text{opt}}\} = \arg \min_{\substack{BW \in (0, \pi) \\ SLL \in (a, 0)}} \int_0^\pi |G_{\text{eff}}(\varphi) - G_{\text{real}}(\varphi)| d\varphi$$

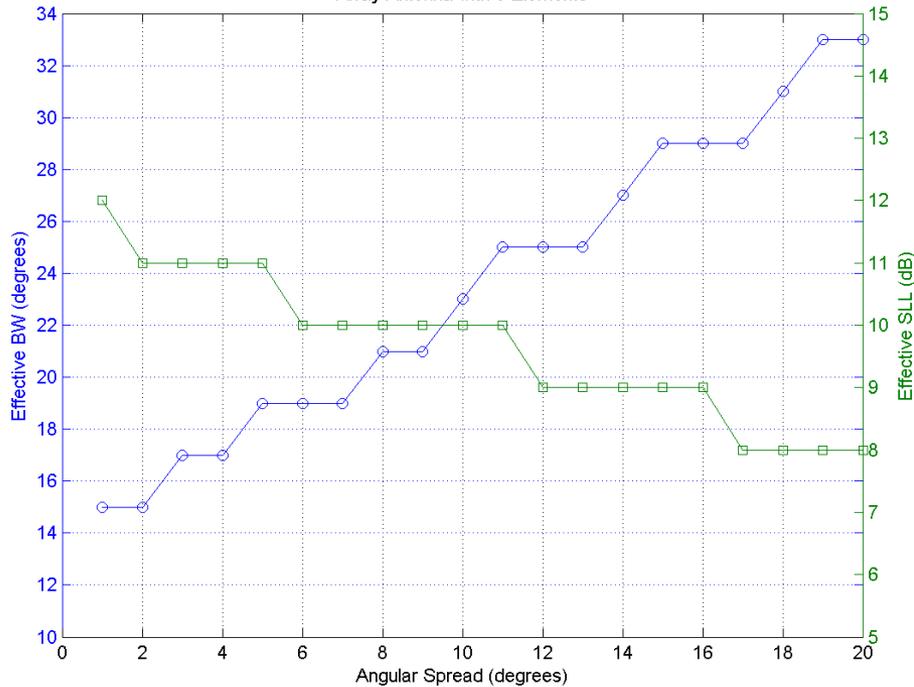
Choosing Effective BW and SLL (1)

- Ideal Radiation Pattern: 8-element array antenna (12° 3dB beamwidth)
- Highly NLOS environment with $AS=20^\circ$
- $BW_{opt} = 33^\circ$, $SLL_{opt} = -8\text{dB}$

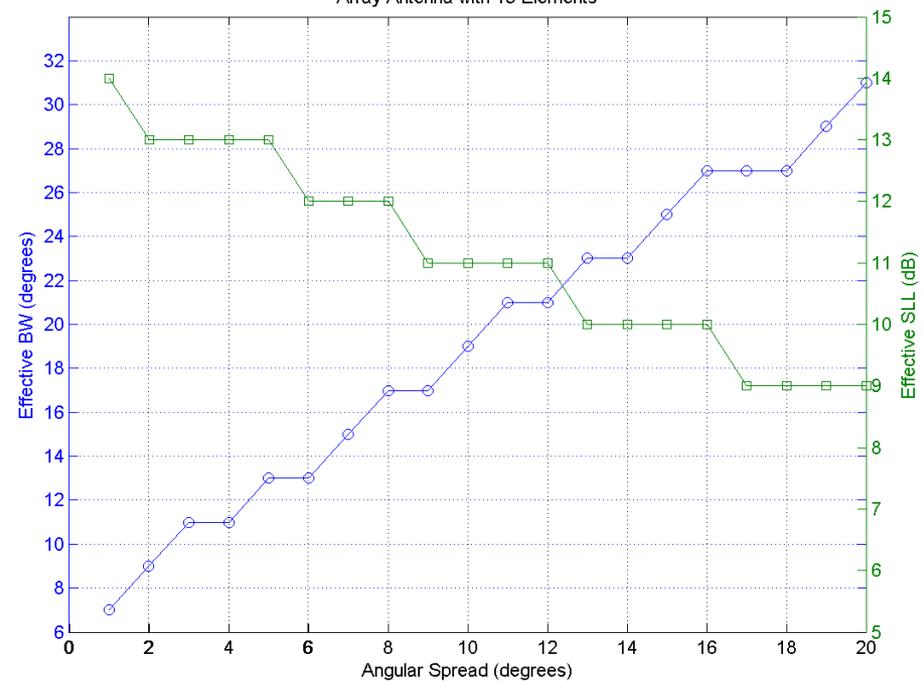


Choosing Effective BW and SLL (2)

Array Antenna with 8 Elements



Array Antenna with 15 Elements





***Thank you for your
attention!!***

